## Mathematics Outcomes Progression 3-7

Supplementary Document





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## **MATHEMATICS PROGRESSION: Grade 3 to 7**

The **Foundational Outcomes** identified in this document represent outcomes determined to be relevant for future learning in mathematics. Decisions about foundational outcomes were made in consultation with teachers, provincial mathematics team, Board and Regional Centre staff. In response to feedback, some changes have been made to the 2020-21 foundational outcomes to ensure continuity of learning within and across grade levels. The foundational outcomes are meant to guide teachers in making decisions about creating learning experiences that will prepare and engage their learners in a responsive way. However, a teacher's professional judgment remains the most important guide to effectively responding to the needs of their learners.

Colour coding has been used to identify outcomes and indicators as foundational (green), optional (orange) or non-foundational (red) for the 2021-2022 school year.

		NUMBER PRO	GRESSION: WHOLE NUMBERS		
TOPIC	MATHEMATICS 3	MATHEMATICS 4	MATHEMATICS 5	MATHEMATICS 6	MATHEMATICS 7
SAYING NUMBER SEQUENCES, MEANINGFUL COUNTING, AND SKIP COUNTING	<ul> <li>N01 Students will be expected to say the number sequence forward and backward by</li> <li>1s through transitions to 1000</li> <li>2s, 5s, 10s, or 100s, using any starting point to 1000</li> <li>3s, using starting points that are multiples of 3 up to 100</li> <li>4s, using starting points that are multiples of 4 up to 100</li> <li>25s, using starting points that are multiples of 25 up to 200.</li> </ul>	<b>N02</b> Students will be expected to compare and order numbers to 10 000.	<b>N01</b> Students will be expected to represent and partition whole numbers to 1 000 000.	<b>N01</b> Students will be expected to demonstrate an understanding of place value for numbers greater than one million and less than one-thousandth.	N07 Students will be expected to compare, order, and position, positive fractions, positive decimals (to thousandths), and whole numbers by using benchmarks, place value, and equivalent fractions and/or decimals.
	<ul> <li>N03 Students will be expected to compare and order numbers up to 1000.</li> <li>N03.01: Place a given set of numbers in ascending or descending order and verify the result using a number chart or other models.</li> <li>N03.02: Create as many different 3-digit numerals as possible, given three different digits. Place the numbers in ascending or descending order.</li> <li>N03.03: Identify errors in a given ordered sequence.</li> </ul>				

	N03.04: Identify missing numbers in parts of a given number chart and on a number line. N03.05: Identify errors in a given number chart and on a number line. N03.06: Place numbers on a number line containing benchmark numbers for the purpose of comparison. N03.07 : Compare numbers based on a variety of methods, and record the comparison using words and symbols (=, > and <).				
REPRESENTING AND PARTITIONING WHOLE NUMBERS	<ul> <li>NO2 Students will be expected to represent and partition numbers to 1000.</li> <li>NO4: Students will be expected to estimate quantities less than 1000 using referents.</li> <li>NO4.01: Estimate the number of groups of ten in a given quantity using 10 as a referent(known quantity).</li> <li>NO4.02: Estimate the number of groups of a hundred in a given quantity using 100 as a referent.</li> <li>NO4.03: Estimate a given quantity by comparing it to a referent.</li> <li>NO4.04: Select an estimate for a given quantity by choosing among three possible choices.</li> <li>NO4.05: Select and justify a referent for determining an estimate for a given quantity.</li> </ul>	<b>N01</b> Students will be expected to represent and partition whole numbers to 10 000.	<b>N01</b> Students will be expected to represent and partition whole numbers to 1 000 000.	N01 Students will be expected to demonstrate an understanding of place value for numbers greater than one million and less than one-thousandth.	N07 Students will be expected to compare, order, and position positive fractions, positive decimals (to thousandths), and whole numbers by using benchmarks, place value, and equivalent fractions and/or decimals.
COMPARING AND ORDERING WHOLE NUMBERS	<ul> <li>N01 Students will be expected to say the number sequence forward and backward by</li> <li>1s through transitions to 1000</li> <li>2s, 5s, 10s, or 100s, using any starting point to 1000</li> <li>3s, using starting points that are multiples of 3 up to 100</li> </ul>	<b>N02</b> Students will be expected to compare and order numbers to 10 000.	<b>N01</b> Students will be expected to represent and partition whole numbers to 1 000 000.	<b>N01</b> Students will be expected to demonstrate an understanding of place value for numbers greater than one million and less than one-thousandth.	<b>N07</b> Students will be expected to compare, order, and position positive fractions, positive decimals (to thousandths), and whole numbers by using benchmarks, place value, and equivalent fractions and/or decimals.

			GRESSION: DECIMAL NUMBERS		
TOPIC	MATHEMATICS 3	MATHEMATICS 4	MATHEMATICS 5	MATHEMATICS 6	MATHEMATICS 7
REPRESENTING DECIMAL NUMBERS	NA	<ul> <li>N09 Students will be expected to describe and represent decimals (tenths and hundredths) concretely, pictorially, and symbolically.</li> <li>N10 Students will be expected to relate decimals to fractions and fractions to decimals (to hundredths).</li> </ul>	<ul> <li>No8 Students will be expected to describe and represent decimals (tenths, hundredths, and thousandths) concretely, pictorially, and symbolically.</li> <li>N09 Students will be expected to relate decimals to fractions and fractions to decimals (to thousandths).</li> <li>N10 Students will be expected to compare and order decimals (to thousandths) by using benchmarks, place value, and equivalent decimals.</li> </ul>	No1 Students will be expected to demonstrate an understanding of place value for numbers greater than one million and less than one-thousandth.	<ul> <li>N04 Students will be expected to demonstrate an understanding of the relationship between positive terminating decimals and positive fractions and between positive repeating decimals (with one or two repeating digits) and positive fractions.</li> <li>N04.01 Predict the decimal representation of a given fraction using patterns. N04.02 Match a given set of fractions to their decimal representations.</li> <li>N04.03 Sort a given set of fractions as repeating or terminating decimals. N04.04 Express a given fraction as a terminating or repeating decimal. N04.05 Express a given repeating decimal as a fraction. N04.07 Provide an example where the decimal representation of a fraction is an approximation of its exact value.</li> <li>N07 Students will be expected to compare, order, and positive fractions, and whole numbers by using benchmarks, place value, and</li> </ul>
COMPARING AND ORDERING DECIMAL NUMBERS	NA	<b>N09</b> Students will be expected to describe and represent decimals (tenths and hundredths) concretely, pictorially, and symbolically.	<b>N08</b> Students will be expected to describe and represent decimals (tenths, hundredths, and thousandths) concretely, pictorially, and symbolically.	<b>N01</b> Students will be expected to demonstrate an understanding of place value for numbers greater than one million and less than one-thousandth.	equivalent fractions and/or decimals. <b>N07</b> Students will be expected to compare, order, and position positive fractions, positive decimals (to thousandths), and whole numbers by using

			N10 Students will be expected to compare and order decimals (to thousandths) by using benchmarks, place value, and equivalent decimals.		benchmarks, place value, and equivalent fractions and/or decimals. NO4 Students will be expected to demonstrate an understanding of the relationship between positive terminating decimals and positive fractions and between positive repeating decimals (with one or two repeating digits) and positive fractions. NO4.01 Predict the decimal representation of a given fraction using patterns. NO4.02 Match a given set of fractions to their decimal representations. NO4.03 Sort a given set of fractions as repeating or terminating decimals. NO4.04 Express a given fraction as a terminating or repeating decimal. NO4.05 Express a given repeating decimal as a fraction. NO4.07 Provide an example where the decimal representation of a fraction is an approximation of its exact value.
PLACE VALUE – DECIMAL NUMBERS	NA	<b>N09</b> Students will be expected to describe and represent decimals (tenths and hundredths) concretely, pictorially, and symbolically.	<ul> <li>N08 Students will be expected to describe and represent decimals (tenths, hundredths, and thousandths) concretely, pictorially, and symbolically.</li> <li>N10 Students will be expected to compare and order decimals (to thousandths) by using benchmarks, place value, and equivalent decimals.</li> </ul>	<b>N01</b> Students will be expected to demonstrate an understanding of place value for numbers greater than one million and less than one-thousandth.	<ul> <li>N07 Students will be expected to compare, order, and position positive fractions, positive decimals (to thousandths), and whole numbers by using benchmarks, place value, and equivalent fractions and/or decimals.</li> <li>N04 Students will be expected to demonstrate an</li> </ul>

		understanding of the relationship between positive terminating decimals and positive fractions and between positive repeating decimals (with one or two repeating digits) and positive fractions.
		N04.01 Predict the decimal representation of a given fraction using patterns. N04.02 Match a given set of fractions to their decimal representations. N04.03 Sort a given set of fractions as repeating or terminating decimals. N04.04 Express a given fraction as a terminating or repeating decimal. N04.05 Express a given repeating decimal as a fraction. N04.06 Express a given terminating decimal as a
		fraction. N04.07 Provide an example where the decimal representation of a fraction is an approximation of its exact value.

NUMBER PROGRESSION: FRACTIONS							
TOPIC	MATHEMATICS 3	MATHEMATICS 4	MATHEMATICS 5	MATHEMATICS 6	MATHEMATICS 7		
REPRESENTING FRACTIONS	<ul> <li>N13 Students will be expected to demonstrate an understanding of fractions by</li> <li>explaining that a fraction represents a part of a whole</li> <li>describing situations in which fractions are used</li> <li>comparing fractions of the same whole with like denominators</li> </ul>	<ul> <li>N08 Students will be expected to demonstrate an understanding of fractions less than or equal to 1 by using concrete, pictorial, and symbolic representations to <ul> <li>name and record fractions for the parts of one whole or a set</li> <li>compare and order fractions</li> <li>model and explain that for different wholes, two identical fractions may not</li> </ul> </li> </ul>	<ul> <li>N07 Students will be expected to demonstrate an understanding of fractions by using concrete, pictorial, and symbolic representations to</li> <li>create sets of equivalent fractions</li> <li>compare and order fractions with like and unlike denominators</li> <li>N09 Students will be expected to relate decimals to fractions</li> </ul>	<ul> <li>N04 Students will be expected to relate improper fractions to mixed numbers and mixed numbers to improper fractions.</li> <li>N06 Students will be expected to demonstrate an understanding of percent (limited to whole numbers) concretely, pictorially, and symbolically.</li> <li>N05 Students will be expected to demonstrate an understanding of ratio,</li> </ul>	<ul> <li>N07 Students will be expected to compare, order, and position positive fractions, positive decimals (to thousandths), and whole numbers by using benchmarks, place value, and equivalent fractions and/or decimals.</li> <li>N04 Students will be expected to demonstrate an understanding of the relationship between</li> </ul>		

		represent the same quantity • provide examples of where fractions are used	and fractions to decimals (to thousandths).	concretely, pictorially, and symbolically.	positive terminating decimals and positive fractions and between positive repeating decimals (with one or two repeating digits) and positive fractions. N04.01 Predict the decimal representation of a given fraction using patterns. N04.02 Match a given set of fractions to their decimal representations. N04.03 Sort a given set of fractions as repeating or terminating decimals. N04.04 Express a given fraction as a terminating or repeating decimal. N04.05 Express a given repeating decimal as a fraction. N04.06 Express a given terminating decimal as a fraction. N04.07 Provide an example where the decimal
COMPARING AND ORDERING FRACTIONS	<ul> <li>N13 Students will be expected to demonstrate an understanding of fractions by</li> <li>explaining that a fraction represents a part of a whole</li> <li>describing situations in which fractions are used comparing fractions of the same whole with like denominators</li> </ul>	<ul> <li>N08 Students will be expected to demonstrate an understanding of fractions less than or equal to 1 by using concrete, pictorial, and symbolic representations to</li> <li>name and record fractions for the parts of one whole or a set</li> <li>compare and order fractions</li> <li>model and explain that for different wholes, two identical fractions may not represent the same quantity</li> <li>provide examples of where fractions are used</li> </ul>	<ul> <li>N07 Students will be expected to demonstrate an understanding of fractions by using concrete, pictorial, and symbolic representations to</li> <li>create sets of equivalent fractions</li> <li>compare and order fractions with like and unlike denominators</li> </ul>	<b>N04</b> Students will be expected to relate improper fractions to mixed numbers and mixed numbers to improper fractions.	representation of a fraction is an approximation of its exact value. SP04 Students will be expected to express probabilities as ratios, fractions, and percents. N07 Students will be expected to compare, order, and position positive fractions, positive decimals (to thousandths), and whole numbers by using benchmarks, place value, and equivalent fractions and/or decimals. N04 Students will be expected to demonstrate an understanding of the relationship between positive terminating decimals and positive fractions and between positive repeating decimals (with one or two

		repeating digits) and positive fractions.
		N04.01 Predict the decimal
		representation of a given
		fraction using patterns.
		N04.02 Match a given set of
		fractions to their decimal
		representations.
		N04.03 Sort a given set of
		fractions as repeating or
		terminating decimals.
		N04.04 Express a given fraction
		as a terminating or repeating
		decimal.
		N04.05 Express a given
		repeating decimal as a fraction.
		N04.06 Express a given
		terminating decimal as a
		fraction.
		N04.07 Provide an example
		where the decimal
		representation of a fraction is
		an approximation of its exact
		value.

	NUMBER PROGRESSION: OPERATIONS ADDITION AND SUBTRACTION							
ΤΟΡΙϹ	MATHEMATICS 3	MATHEMATICS 4	MATHEMATICS 5	MATHEMATICS 6	MATHEMATICS 7			
ADDITION AND SUBTRACTION – BASIC FACTS	<b>N10</b> Students will be expected to apply mental mathematics strategies and number properties to develop quick recall of basic addition facts to 18 and related basic subtraction facts.	Basic addition and subtraction facts should be under control and students are expected to recall them when performing addition and subtraction of larger numbers.	Basic addition and subtraction facts should be under control and students are expected to recall them when performing addition and subtraction of larger numbers.	Basic addition and subtraction facts should be under control and students are expected to recall them when performing addition and subtraction of larger numbers.	Basic addition and subtraction facts should be under control and students are expected to recall them when performing addition and subtraction of larger numbers.			
ADDITION AND SUBTRACTION MENTAL MATHEMATICS AND ESTIMATION	<ul> <li>N06 Students will be expected to describe and apply mental mathematics strategies for adding 2 two-digit numerals.</li> <li>N06.01: Explain mental mathematics strategies that could be used to determine a sum.</li> <li>Ten and some more</li> <li>Tens and some more</li> <li>Quick addition</li> </ul>	<ul> <li>N03 Students will be expected to demonstrate an understanding of addition and subtraction of numbers with answers to 10 000 (limited to three- and four-digit numerals) by</li> <li>using personal strategies for adding and subtracting</li> <li>estimating sums and differences</li> <li>solving problems involving addition and subtraction</li> </ul>	<b>N02</b> Students will be expected to use estimation strategies, including front-end, front-end adjusted, rounding, and compatible numbers in problem-solving contexts.	<b>N02</b> Students will be expected to solve problems involving whole numbers and decimal numbers.	<b>N02</b> Students will be expected to demonstrate an understanding of the addition, subtraction, multiplication, and division of decimals to solve problems (for more than one-digit divisors or more than two-digit multipliers, the use of technology is expected).			

• Addition facts to 10 applied			
to multiples of 10	N11 Students will be expected		
<ul> <li>Addition on the hundred</li> </ul>	to demonstrate an		
chart	understanding of addition and		
<ul> <li>Adding on</li> </ul>	subtraction of decimals		
Make ten	(limited to hundredths) by		
<ul> <li>Compensation</li> </ul>	<ul> <li>estimating sums and</li> </ul>		
<ul> <li>Compatible numbers</li> </ul>	differences		
N06.02: Use and describe a	<ul> <li>using mental mathematics</li> </ul>		
personal strategy for	strategies to solve		
determining a sum.	problems		
N06.03: Determine a sum of	<ul> <li>using personal strategies to</li> </ul>		
two 2-digit numerals efficiently,	determine sums and		
using mental mathematics	differences		
strategies.			
N07 Students will be expected			
to describe and apply mental			
mathematics strategies for			
subtracting 2 two-digit			
numerals.			
N07.01: Explain mental			
mathematics strategies that			
could be used to determine a			
difference.			
<ul> <li>Facts with minuends of 10</li> </ul>			
or less applied to multiples			
of 10			
Quick subtraction			
• Subtraction on the hundred			
chart			
Compensation			
Back through ten			
N07.02: Use and describe a			
personal strategy for			
determining a difference.			
N07.03: Determine a difference			
of two 2-digit numerals			
efficiently, using mental			
mathematics strategies			
-			
N08 Students will be expected			
to apply estimation strategies			
to predict sums and differences			
of one-, two-, and three-digit			
numerals in a problem-solving			
context.			
CONCEXL.			
NOQ 01, Evaloin estimation			
N08.01: Explain estimation			
strategies that could be used to			

determine an approximate sum or difference. N08.02: Use and describe a strategy for determining an estimate. N08.03: Estimate the solution for a given story problem involving the sum or difference of up to two 3-digit numerals.		
<b>N10</b> Students will be expected to apply mental mathematics strategies and number properties to develop quick recall of basic addition facts to 18 and related basic subtraction facts.		

TOPIC	MATHEMATICS 3	MATHEMATICS 4	MATHEMATICS 5	MATHEMATICS 6	MATHEMATICS 7
ADDITION AND SUBTRACTION -CALCULATIONS	<ul> <li>N09 Students will be expected to demonstrate an understanding of addition and subtraction of numbers (limited to one-, two-, and three-digit numerals) with answers to 1000 by         <ul> <li>using personal strategies for adding and subtracting with and without the support of manipulatives</li> <li>creating and solving problems in context that involve addition and subtraction of numbers concretely, pictorially, and symbolically</li> </ul> </li> <li>N09.01: Model the addition of two or more given numbers using concrete or visual representations and record the process symbolically.</li> <li>N09.02: Model the subtraction of two given numbers using concrete or visual representations and record the process symbolically.</li> </ul>	<ul> <li>N03 Students will be expected to demonstrate an understanding of addition and subtraction of numbers with answers to 10 000 (limited to three- and four-digit numerals) by</li> <li>using personal strategies for adding and subtracting</li> <li>estimating sums and differences</li> <li>solving problems involving addition and subtraction</li> <li>N11 Students will be expected to demonstrate an understanding of addition and subtraction</li> <li>N11 Students will be expected to demonstrate an understanding of addition and subtraction estimating sums and differences</li> <li>using mental mathematics strategies to solve problems</li> <li>using personal strategies to determine sums and differences</li> </ul>	<ul> <li>N02 Students will be expected to use estimation strategies, including front-end, front-end adjusted, rounding, and compatible numbers in problem-solving contexts.</li> <li>N11 Students will be expected to demonstrate an understanding of addition and subtraction of decimals (limited to thousandths).</li> </ul>	<ul> <li>N02 Students will be expected to solve problems involving whole numbers and decimal numbers.</li> <li>N09 Students will be expected to explain and apply the order of operations, excluding exponents, with and without technology (limited to whole numbers).</li> </ul>	<ul> <li>N02 Students will be expected to demonstrate an understanding of the addition, subtraction, multiplication, and division of decimals to solve problems (for more than one-digit divisors or more than two-digit multipliers, the use of technology is expected).</li> <li>N05 Students will be expected to demonstrate an understanding of adding and subtracting positive fractions and mixed numbers, with like and unlike denominators, concretely, pictorially, and symbolically (limited to positive sums and differences).</li> <li>N06 Students will be expected to demonstrate an understanding of addition and symbolically (limited to positive sums and differences).</li> <li>N06 Students will be expected to demonstrate an understanding of addition and subtraction of integers, concretely, pictorially, and symbolically.</li> </ul>

<ul> <li>N09.03: Create an addition or subtraction story problem for a given solution.</li> <li>N09.04: Determine the sum of two given numbers using a personal strategy, e.g., for 326 + 48, record 300 + 60 + 14.</li> <li>N09.05: Determine the difference of two given numbers using a personal strategy, e.g., for 127 - 38, record 2 + 80 + or 127 - 20 - 10 - 8.</li> <li>N09.06: Solve a given problem involving the sum or difference of two given numbers.</li> </ul>				
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	NUMBER PROGRESSION: OPERATIONS MULTIPLICATION AND DIVISION								
ТОРІС	MATHEMATICS 3	MATHEMATICS 4	MATHEMATICS 5	MATHEMATICS 6	MATHEMATICS 7				
MULTIPLICATION AND DIVISION – BASIC FACTS	<ul> <li>N01 Students will be expected to say the number sequence forward and backward by</li> <li>1s through transitions to 1000</li> <li>2s, 5s, 10s, or 100s, using any starting point to 1000</li> <li>3s, using starting points that are multiples of 3 up to 100</li> <li>4s, using starting points that are multiples of 4 up to 100</li> <li>25s, using starting points that are multiples of 25 up to 200.</li> <li>N11 Students will be expected to demonstrate an understanding of multiplication to 5 × 5 by</li> <li>representing and explaining multiplication using equal grouping and arrays</li> <li>creating and solving problems in context that involves multiplication</li> </ul>	<ul> <li>N04 Students will be expected to apply and explain the properties of 0 and 1 for multiplication and the property of 1 for division.</li> <li>N05 Students will be expected to describe and apply mental mathematics strategies, to recall basic multiplication facts to 9 × 9, and to determine related division facts.</li> </ul>	N03 Students will be expected to describe and apply mental mathematics strategies and number properties to recall, with fluency, answers for basic multiplication facts to 81 and related division facts.	Basic multiplication and division facts should be under control and students are expected to recall them when performing multiplication and division. <b>N02</b> Students will be expected to solve problems involving whole numbers and decimal numbers.	Basic multiplication and division facts should be under control and students are expected to recall them when performing multiplication and division.				

	<ul> <li>modelling multiplication</li> </ul>				
	<ul> <li>Instacting interpretation using concrete and visual representations and recording the process symbolically</li> <li>relating multiplication to repeated addition</li> <li>relating multiplication to division</li> </ul>				
	<ul> <li>N12 Students will be expected to demonstrate an understanding of division by</li> <li>representing and explaining division using equal sharing and equal grouping</li> <li>creating and solving problems in context that involve equal sharing and equal grouping</li> <li>modelling equal sharing and equal grouping using concrete and visual representations, and recording the process symbolically</li> <li>relating division to repeated subtraction</li> <li>relating division to multiplication</li> <li>(Limited to division related to multiplication facts up to 5 × 5.)</li> </ul>				
MULTIPLICATION AND DIVISION – MENTAL MATHEMATICS AND ESTIMATIONS		<ul> <li>N04 Students will be expected to apply and explain the properties of 0 and 1 for multiplication and the property of 1 for division.</li> <li>N05 Students will be expected to describe and apply mental mathematics strategies, to recall basic multiplication facts to 9 × 9, and to determine related division facts.</li> <li>N06 Students will be expected to demonstrate an understanding of multiplication (one-, two-, or three-digit by one-digit numerals) to solve problems by</li> </ul>	<ul> <li>N03 Students will be expected to describe and apply mental mathematics strategies and number properties to recall, with fluency, answers for basic multiplication facts to 81 and related division facts.</li> <li>N04 Students will be expected to apply mental mathematics strategies for multiplication, including <ul> <li>multiplying by multiples of 10, 100, and 1000</li> <li>halving and doubling</li> <li>using the distributive property</li> </ul> </li> </ul>	<ul> <li>N02 Students will be expected to solve problems involving whole numbers and decimal numbers.</li> <li>N08 Students will be expected to demonstrate an understanding of multiplication and division of decimals (one-digit whole number multipliers and one-digit natural number divisors).</li> </ul>	N01 Students will be expected to determine and explain why a number is divisible by 2, 3, 4, 5, 6, 8, 9, or 10, and why a number cannot be divided by 0. N01.01 Determine if a given number is divisible by 2, 3, 4, 5, 6, 8, 9, or 10, and explain why. N01.02 Sort a given set of numbers based upon their divisibility using organizers such as Venn and Carroll diagrams. N01.03 Determine the factors of a given number using the divisibility rules.

	<ul> <li>using personal strategies for multiplication, with and without concrete materials</li> <li>using arrays to represent multiplication</li> <li>connecting concrete representations to symbolic representations</li> <li>estimating products</li> <li>applying the distributive property</li> <li>NO7 Students will be expected to demonstrate an understanding of division (one-digit divisor and up to two-digit dividend) to solve problems by</li> <li>using personal strategies for dividing, with and without concrete materials</li> <li>estimating quotients</li> <li>relating division to multiplication</li> </ul>	N05 Students will be expected to demonstrate, with and without concrete materials, an understanding of multiplication (two-digit by two-digit) to solve problems. N06 Students will be expected to demonstrate, with and without concrete materials, an understanding of division (three-digit by one-digit), and interpret remainders to solve problems.		<ul> <li>N01.04 Explain, using an example, why numbers cannot be divided by 0.</li> <li>N02 Students will be expected to demonstrate an understanding of the addition, subtraction, multiplication, and division of decimals to solve problems (for more than one-digit divisors or more than two-digit multipliers, the use of technology is expected).</li> <li>N04 Students will be expected to demonstrate an understanding of the relationship between positive terminating decimals and positive fractions and between positive repeating decimals (with one or two repeating digits) and positive fractions.</li> <li>N04.01 Predict the decimal representation of a given fraction using patterns. N04.02 Match a given set of fractions to their decimal representations.</li> <li>N04.03 Sort a given set of fractions as repeating or terminating decimals.</li> <li>N04.05 Express a given fraction.</li> <li>N04.05 Express a given fraction.</li> <li>N04.05 Express a given fraction.</li> <li>N04.07 Provide an example where the decimal representation of a fraction.</li> </ul>
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MULTIPLICATION	N11 Students will be expected	N04 Students will be expected	N03 Students will be expected	N02 Students will be expected	N01 Students will be expected
AND DIVISION -	to demonstrate an	to apply and explain the	to describe and apply mental	to solve problems involving	to determine and explain why a
CALCULATIONS	understanding of multiplication	properties of 0 and 1 for	mathematics strategies and	whole numbers and decimal	number is divisible by 2, 3, 4, 5,
	to 5 × 5 by	multiplication and the property	number properties to recall,	numbers.	6, 8, 9, or 10, and why a
	• representing and explaining	of 1 for division.	with fluency, answers for basic		number cannot be divided by 0
	multiplication using equal		multiplication facts to 81 and	N03 Students will be	N01.01 Determine if a given
	grouping and arrays	N05 Students will be expected	related division facts.	expected to demonstrate an	number is divisible by 2, 3, 4, 5,
	<ul> <li>creating and solving</li> </ul>	to describe and apply mental		understanding of factors and	6, 8, 9, or 10, and explain why.
	problems in context that	mathematics strategies, to	N04 Students will be expected	multiples by	NO1 02 Cart a since act of
	involves multiplication	recall basic multiplication facts	to apply mental mathematics	<ul> <li>determining multiples and factors of numbers less</li> </ul>	N01.02 Sort a given set of
	<ul> <li>modelling multiplication using concrete and visual</li> </ul>	to 9 × 9, and to determine related division facts.	strategies for multiplication, including	than 100	numbers based upon their divisibility using organizers
	representations and	Telated division facts.	<ul> <li>multiplying by multiples of</li> </ul>	<ul> <li>identifying prime and</li> </ul>	such as Venn and Carroll
	recording the process	N06 Students will be expected	10, 100, and 1000	composite numbers	diagrams.
	symbolically	to demonstrate an	<ul> <li>halving and doubling</li> </ul>	<ul> <li>solving problems using</li> </ul>	N01.03 Determine the factors
	<ul> <li>relating multiplication to</li> </ul>	understanding of multiplication	<ul> <li>using the distributive</li> </ul>	multiples and factors	of a given number using the
	repeated addition	(one-, two-, or three-digit by	property	maniples and factors	divisibility rules.
	<ul> <li>relating multiplication to</li> </ul>	one-digit numerals) to solve	p. opercy	N09 Students will be expected	N01.04 Explain, using an
	division	problems by	N05 Students will be expected	to explain and apply the order	example, why numbers cannot
		<ul> <li>using personal strategies</li> </ul>	to demonstrate, with and	of operations, excluding	be divided by 0.
		for multiplication, with and	without concrete materials, an	exponents, with and without	
	N12 Students will be expected	without concrete materials	understanding of multiplication	technology (limited to whole	N02 Students will be expected
	to demonstrate an	<ul> <li>using arrays to represent</li> </ul>	(two-digit by two-digit) to solve	numbers).	to demonstrate an
	understanding of division by	multiplication	problems.	,	understanding of the addition,
	• representing and explaining	<ul> <li>connecting concrete</li> </ul>		N08 Students will be expected	subtraction, multiplication, and
	division using equal sharing	representations to symbolic	N06 Students will be expected	to demonstrate an	division of decimals to solve
	and equal grouping	representations	to demonstrate, with and	understanding of multiplication	problems (for more than
	<ul> <li>creating and solving</li> </ul>	<ul> <li>estimating products</li> </ul>	without concrete materials, an	and division of decimals	one-digit divisors or more than
	problems in context that	<ul> <li>applying the distributive</li> </ul>	understanding of division	(one-digit whole number	two-digit multipliers, the use of
	involve equal sharing and equal grouping	property	(three-digit by one-digit), and	multipliers and one-digit	technology is expected).
	<ul> <li>modelling equal sharing</li> </ul>		interpret remainders to solve	natural number divisors).	
	<ul> <li>modelling equal sharing and equal grouping using</li> </ul>	N07 Students will be expected	problems.		N03 Students will be expected
	concrete and visual	to demonstrate an			to solve problems involving
	representations, and	understanding of division			percents from 1% to 100%
	recording the process	(one-digit divisor and up to			(limited to whole numbers).
	symbolically	two-digit dividend) to solve			
	<ul> <li>relating division to</li> </ul>	problems by			
	repeated subtraction	• using personal strategies			
	<ul> <li>relating division to</li> </ul>	for dividing, with and			
	multiplication	without concrete materials			
	(Limited to division related to	<ul> <li>estimating quotients</li> </ul>			
	multiplication facts up to 5 ×	<ul> <li>relating division to</li> </ul>			
	5.)	multiplication			

	NUMBER PROGRESSION: RATIO, PERCENT, AND INTEGERS							
ΤΟΡΙϹ	MATHEMATICS 3	MATHEMATICS 4	MATHEMATICS 5	MATHEMATICS 6	MATHEMATICS 7			
RATIO	<ul> <li>N11 Students will be expected to demonstrate an understanding of multiplication to 5 × 5 by</li> <li>representing and explaining multiplication using equal grouping and arrays</li> <li>creating and solving problems in context that involves multiplication</li> <li>modelling multiplication</li> <li>modelling multiplication using concrete and visual representations and recording the process symbolically</li> <li>relating multiplication to repeated addition</li> <li>relating multiplication to division</li> <li>N13 Students will be expected to demonstrate an understanding of fractions by</li> <li>explaining that a fraction represents a part of a whole</li> <li>describing situations in which fractions are used</li> <li>comparing fractions of the same whole with like</li> </ul>	<ul> <li>N05 Students will be expected to describe and apply mental mathematics strategies, to recall basic multiplication facts to 9 × 9, and to determine related division facts.</li> <li>N06 Students will be expected to demonstrate an understanding of multiplication (one-, two-, or three-digit by one-digit numerals) to solve problems by <ul> <li>using personal strategies for multiplication, with and without concrete materials</li> <li>using arrays to represent multiplication</li> <li>connecting concrete representations to symbolic representations</li> <li>estimating products</li> <li>applying the distributive property</li> </ul> </li> <li>N08 Students will be expected to demonstrate an understanding of fractions less than or equal to 1 by using concrete, pictorial, and symbolic representations to</li> <li>name and record fractions for the parts of one whole or a set</li> <li>compare and order fractions</li> <li>model and explain that for different wholes, two identical fractions may not represent the same quantity</li> <li>provide examples of where fractions are used</li> </ul>	<ul> <li>N05 Students will be expected to demonstrate, with and without concrete materials, an understanding of multiplication (two-digit by two-digit) to solve problems.</li> <li>N07 Students will be expected to demonstrate an understanding of fractions by using concrete, pictorial, and symbolic representations to <ul> <li>create sets of equivalent fractions</li> <li>compare and order fractions with like and unlike denominators</li> </ul> </li> <li>N09 Students will be expected to relate decimals to fractions and fractions to decimals (to thousandths)</li> </ul>	N05 Students will be expected to demonstrate an understanding of ratio, concretely, pictorially, and symbolically.	SP04 Students will be expected to express probabilities as ratios, fractions, and percents.			

PERCENT	<ul> <li>N09 Students will be expected to describe and represent decimals (tenths and hundredths) concretely, pictorially, and symbolically.</li> <li>N10 Students will be expected to relate decimals to fractions and fractions to decimals (to hundredths).</li> </ul>	<ul> <li>N08 Students will be expected to describe and represent decimals (tenths, hundredths, and thousandths) concretely, pictorially, and symbolically.</li> <li>N09 Students will be expected to relate decimals to fractions and fractions to decimals (to thousandths).</li> <li>N10 Students will be expected to compare and order decimals (to thousandths) by using benchmarks, place value, and equivalent decimals.</li> </ul>	N06 Students will be expected to demonstrate an understanding of percent (limited to whole numbers) concretely, pictorially, and symbolically.	<ul> <li>N03 Students will be expected to solve problems involving percents from 1% to 100% (limited to whole numbers).</li> <li>SP04 Students will be expected to express probabilities as ratios, fractions, and percents.</li> </ul>
INTEGERS			<b>N07</b> Students will be expected to demonstrate an understanding of integers contextually, concretely, pictorially, and symbolically.	<b>N06</b> Students will be expected to demonstrate an understanding of addition and subtraction of integers, concretely, pictorially, and symbolically.

	PATTERNS AND RELATIONS PROGRESSION						
TOPIC	MATHEMATICS 3	MATHEMATICS 4	MATHEMATICS 5	MATHEMATICS 6	MATHEMATICS 7		
REPEATING PATTERNS							
INCREASING PATTERNS	<b>PR01</b> Students will be expected to demonstrate an understanding of increasing patterns by describing, extending, comparing, and creating numerical (numbers to 1000) patterns and non-numerical patterns using manipulatives, diagrams, sounds, and actions.	<ul> <li>PR01 Students will be expected to identify and describe patterns found in tables and charts, including a multiplication chart.</li> <li>PR02 Students will be expected to translate among different representations of a pattern (a table, a chart, or concrete materials).</li> <li>PR03 Students will be expected to represent, describe, and extend patterns and relationships, using charts and tables, to solve problems.</li> <li>PR04 Students will be expected to identify and explain mathematical relationships, solve problems.</li> </ul>	<b>PR01</b> Students will be expected to determine the pattern rule to make predictions about subsequent terms.	<ul> <li>PR01 Students will be expected to demonstrate an understanding of the relationships within tables of values to solve problems.</li> <li>PR02 Students will be expected to represent and describe patterns and relationships, using graphs and tables.</li> </ul>	<ul> <li>PR01 Students will be expected to demonstrate an understanding of oral and written patterns and their equivalent linear relations.</li> <li>PR02 Students will be expected to create a table of values from a linear relation, graph the table of values, and analyze the graph to draw conclusions and solve problems.</li> </ul>		

		using charts and diagrams, to solve problems. PR04.01 Complete a given Carroll diagram to solve a problem. PR04.02 Determine where new elements belong is a given Carroll diagram. PR04.03 Solve a given problem using a Carroll diagram. PR04.04 Identify a sorting rule for a given Venn diagram. PR04.05 Describe the relationship shown in a given Venn diagram when the circles overlap, when one circle is contained in the other, and when the circles are separate. PR04.06 Determine where new elements belong in a given Venn diagram. PR04.07 Solve a given problem by using a chart or diagram to identify mathematical relationships.			
DECREASING PATTERNS	<b>PR02</b> Students will be expected to demonstrate an understanding of decreasing patterns by describing, extending, comparing, and creating numerical (numbers to 1000) patterns and non-numerical patterns using manipulatives, diagrams, sounds, and actions.	<ul> <li>PR01 Students will be expected to identify and describe patterns found in tables and charts, including a multiplication chart.</li> <li>PR02 Students will be expected to translate among different representations of a pattern (a table, a chart, or concrete materials).</li> <li>PR03 Students will be expected to represent, describe, and extend patterns and relationships, using charts and tables, to solve problems.</li> </ul>	<b>PR01</b> Students will be expected to determine the pattern rule to make predictions about subsequent terms	<ul> <li>PR01 Students will be expected to demonstrate an understanding of the relationships within tables of values to solve problems.</li> <li>PR02 Students will be expected to represent and describe patterns and relationships, using graphs and tables.</li> </ul>	<ul> <li>PR01 Students will be expected to demonstrate an understanding of oral and written patterns and their equivalent linear relations.</li> <li>PR02 Students will be expected to create a table of values from a linear relation, graph the table of values, and analyze the graph to draw conclusions and solve problems.</li> </ul>

		<ul> <li>PR04 Students will be expected to identify and explain mathematical relationships, using charts and diagrams, to solve problems.</li> <li>PR04.01 Complete a given Carroll diagram to solve a problem.</li> <li>PR04.02 Determine where new elements belong is a given Carroll diagram.</li> <li>PR04.03 Solve a given problem using a Carroll diagram.</li> <li>PR04.04 Identify a sorting rule for a given Venn diagram.</li> <li>PR04.05 Describe the relationship shown in a given Venn diagram when the circles overlap, when one circle is contained in the other, and when the circles are separate.</li> <li>PR04.06 Determine where new elements belong in a given Venn diagram.</li> </ul>			
EQUALITY	<b>PR03</b> Students will be expected to solve one-step addition and subtraction equations involving symbols representing an unknown number.	<ul> <li>PR05 Students will be expected to express a given problem as an equation in which a symbol is used to represent an unknown number.</li> <li>PR06 Students will be expected to solve one-step equations involving a symbol to represent an unknown number.</li> </ul>	<b>PR02</b> Students will be expected to solve problems involving single-variable, one-step equations with whole number coefficients and whole number solutions.	<ul> <li>PR01 Students will be expected to demonstrate an understanding of the relationships within tables of values to solve problems.</li> <li>PR02 Students will be expected to represent and describe patterns and relationships, using graphs and tables.</li> <li>PR03 Students will be expected to represent generalizations arising from number relationships using equations with letter variables.</li> </ul>	<ul> <li>PR01 Students will be expected to demonstrate an understanding of oral and written patterns and their equivalent linear relations.</li> <li>PR02 Students will be expected to create a table of values from a linear relation, graph the table of values, and analyze the graph to draw conclusions and solve problems.</li> <li>PR03 Students will be expected to demonstrate an</li> </ul>

		<b>PR04</b> Students will be expected to demonstrate and explain the meaning of preservation of equality concretely, pictorially, and symbolically.	<ul> <li>understanding of preservation of equality by</li> <li>modelling preservation of equality, concretely, pictorially, and symbolically</li> <li>applying preservation of equality to solve equations</li> </ul>
			PR03.01 Model the preservation of equality for each of the four operations, using concrete materials and/or pictorial representations; explain the process orally; and record the process symbolically. PR03.02 Write equivalent forms of a given equation by applying the preservation of equality, and verify using concrete materials (e.g., $3b =$ 12 is equivalent to $3b + 5 = 12$ + 5 or $2r = 7$ is equivalent to 3(2r) = 3(7). PR03.03 Solve a given problem by applying preservation of equality.
			<ul> <li>PR04 Students will be expected to explain the difference between an expression and an equation.</li> <li>PR05 Students will be expected to evaluate an expression given the value of the variable(s).</li> </ul>

VARIABLES	<b>PR03</b> Students will be expected to solve one-step addition and subtraction equations involving symbols representing an unknown number.	<b>PR05</b> Students will be expected to express a given problem as an equation in which a symbol is used to represent an unknown number.	<b>PR02</b> Students will be expected to solve problems involving single-variable, one-step equations with whole number coefficients and whole number solutions.	<b>PR01</b> Students will be expected to demonstrate an understanding of the relationships within tables of values to solve problems.	<b>PR01</b> Students will be expected to demonstrate an understanding of oral and written patterns and their equivalent linear relations.
		<b>PR06</b> Students will be expected to solve one-step equations involving a symbol to represent an unknown number.		<b>PR02</b> Students will be expected to represent and describe patterns and relationships, using graphs and tables.	<b>PR02</b> Students will be expected to create a table of values from a linear relation, graph the table of values, and analyze the

		<ul> <li>PR03 Students will be expected to represent generalizations arising from number relationships using equations with letter variables.</li> <li>PR04 Students will be expected to demonstrate and explain the meaning of preservation of equality concretely, pictorially, and symbolically.</li> </ul>	<ul> <li>graph to draw conclusions and solve problems.</li> <li>PR03 Students will be expected to demonstrate an understanding of preservation of equality by <ul> <li>modelling preservation of equality, concretely, pictorially, and symbolically</li> <li>applying preservation of equality to solve equations</li> </ul> </li> </ul>
			PR03.01 Model the preservation of equality for each of the four operations, using concrete materials and/or pictorial representations; explain the process orally; and record the process symbolically. PR03.02 Write equivalent forms of a given equation by applying the preservation of equality, and verify using concrete materials (e.g., 3b = 12 is equivalent to 3b + 5 = 12 + 5 or 2r = 7 is equivalent to 3(2r) = 3(7). PR03.03 Solve a given problem by applying preservation of equality.
			<ul> <li>PR04 Students will be expected to explain the difference between an expression and an equation.</li> <li>PR05 Students will be expected to evaluate an expression given the value of the variable(s).</li> </ul>
			<b>PR06</b> Students will be expected to model and solve, concretely, pictorially, and symbolically, problems that can be represented by one-step linear equations of the form x + a = b, where a and b are integers.

		<b>PR07</b> Students will be expected to model and solve, concretely, pictorially, and symbolically, where a, b, and c are whole numbers, problems that can be represented by linear equations of the form $ax + b =$ c; $ax = b$ ; $x \div a = b, a \neq 0$
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	MEASUREMENT PROGRESSION						
ТОРІС	MATHEMATICS 3	MATHEMATICS 4	MATHEMATICS 5	MATHEMATICS 6	MATHEMATICS 7		
MEASUREMENT - LENGTH	<ul> <li>MATHEMATICS 3</li> <li>M03 Students will be expected to demonstrate an understanding of measuring length (cm, m) by         <ul> <li>selecting and justifying referents for the units centimetre or metre (cm, m)</li> <li>modelling and describing the relationship between the units centimetre or metre (cm, m)</li> <li>estimating length using referents</li> <li>measuring and recording length, width, and height</li> </ul> </li> <li>M05 Students will be expected to demonstrate an understanding of perimeter of regular, irregular, and composite shapes by         <ul> <li>estimating perimeter using referents for centimetre or metre (cm, m)</li> <li>estimating perimeter using referents for centimetre or a given perimeter (cm, m)</li> <li>create different shapes for a given perimeter (cm, m) to demonstrate that many shapes are possible for a perimeter</li> </ul> </li> </ul>		<ul> <li>MO2 Students will be expected to demonstrate an understanding of measuring length (mm) by</li> <li>selecting and justifying referents for the unit millimetre (mm)</li> <li>modelling and describing the relationship between millimetre (cm) units, and between millimetre (mm) and metre (m) units</li> </ul>				

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	M05.01: Measure and record the perimeter of a given regular shape and explain the strategy used. M05.02: Measure and record			
	the perimeter of a given irregular or composite shape			
	and explain the strategy used. M05.03: Construct a shape for a given perimeter (cm, m).			
	M05.04: Construct or draw more than one shape for the			
	same given perimeter. M05.05: Estimate the perimeter of a given shape			
	(cm, m) using personal referents.			
MEASUREMENT – PERIMETER		<b>M01</b> Students will be expected to design and construct different rectangles, given a perimeter or an area or both (whole numbers), and make generalizations.	<ul> <li>M03 Students will be expected to develop and apply a formula for determining the</li> <li>perimeter of polygons</li> <li>area of rectangles</li> <li>volume of right rectangular prisms</li> </ul>	
MEASUREMENT - MASS	<b>M04</b> Students will be expected to demonstrate an			
	understanding of measuring			
	<ul><li>mass (g, kg) by</li><li>selecting and justifying</li></ul>			
	referents for the units gram and kilogram (g, kg)			
	<ul> <li>modelling and describing</li> </ul>			
	the relationship between the units gram and			
	kilogram (g, kg)			
	<ul> <li>estimating mass using referents</li> </ul>			
	measuring and recording			
	mass M04.01: Provide a personal			
	referent for one gram and explain the choice.			
	M04.02: Provide a personal			
	referent for one kilogram and explain the choice.			
	M04.03: Match a given			
	standard unit to a given			
	referent. M04.04: Explain the			
1	relationship between 1000			

	· · · · · ·			1
	grams and 1 kilogram using a			
	model.			
	M04.05: Estimate the mass of a			
	given object using personal			
	referents.			
	M04.06: Measure, using a			
	balance scale, and record the			
	mass of given everyday objects			
	using the units gram (g) and			
	kilogram (kg).			
	M04.07: Provide examples of			
	3-D objects that have a mass of			
	approximately 1 g, 100 g, and 1			
	kg.			
	M04.08: Determine the mass			
	of two given similar objects			
	with different masses and			
	explain the results.			
	M04.09: Determine the mass			
	of an object, change its shape,			
	re-measure its mass and			
	explain the results			
MEASUREMENT		M03 Students will be expected	M03 Students will be expected	
- VOLUME		to demonstrate an	to develop and apply a formula	
		understanding of volume by	for determining the	
		<ul> <li>selecting and justifying</li> </ul>	<ul> <li>perimeter of polygons</li> </ul>	
		referents for cubic	<ul> <li>area of rectangles</li> </ul>	
		centimetre (cm <sup>3</sup> ) or cubic	• volume of right rectangular	
		metre (m <sup>3</sup> ) units	prisms	
		<ul> <li>estimating volume using</li> </ul>		
		referents for cubic		
		centimetre (cm <sup>3</sup> ) or cubic		
		metre (m <sup>3</sup> )		
		<ul> <li>measuring and recording</li> </ul>		
		volume (cm <sup>3</sup> or m <sup>3</sup> )		
		<ul> <li>constructing rectangular</li> </ul>		
		prisms for a given volume		
MEASUREMENT		M04 Students will be expected		
- CAPACITY		to demonstrate an		
		understanding of capacity by		
		<ul> <li>describing the relationship</li> </ul>		
		between millilitre (mL) and		
		litre (L) units		
		<ul> <li>selecting and justifying</li> </ul>		
		referents for millilitre (mL)		
		and litre (L) units		
		<ul> <li>estimating capacity using</li> </ul>		
		referents for millilitre (mL)		
		and litre (L)		
		<ul> <li>measuring and recording</li> </ul>		
		capacity (mL or L)		
			1	

MEASUREMENT - AREA		<b>M03</b> Students will be expected to demonstrate an understanding of area of regular and irregular 2-D	<b>M01</b> Students will be expected to design and construct different rectangles, given a perimeter	<ul> <li>M03 Students will be expected to develop and apply a formula for determining the</li> <li>perimeter of polygons</li> </ul>	<b>M02</b> Students will be expected to develop and apply a formula for determining the area of triangles, parallelograms, and
		<ul> <li>shapes by</li> <li>recognizing that area is measured in square units</li> <li>selecting and justifying referents for the units square centimetre (cm<sup>2</sup>) or square metre (m<sup>2</sup>)</li> <li>estimating area using referents for cm<sup>2</sup> or m<sup>2</sup></li> <li>determining and recording area (cm<sup>2</sup> or m<sup>2</sup>)</li> <li>constructing different rectangles for a given area (cm<sup>2</sup> or m<sup>2</sup>) in order to demonstrate that many different rectangles may have the same area</li> </ul>	or an area or both (whole numbers), and make generalizations.	<ul> <li>area of rectangles</li> <li>volume of right rectangular prisms</li> </ul>	circles.
MEASUREMENT - TIME	M01 Students will be expected to relate the passage of time to common activities using non-standard and standard units (minutes, hours, days, weeks, months, years). M01.01: Select and use a non-standard unit of measure, such as television shows or pendulum swings, to measure the passage of time and explain the choice. M01.02: Identify activities that can or cannot be accomplished in minutes, hours, days, weeks, months, and years. M01.03: Provide personal referents for minutes and hours. M01.04: Select and use a standard unit of measure, such as minutes, hours, days, weeks, and months to measure the passage of time and explain the choice.	M01 Students will be expected to read and record time using digital and analog clocks, including 24-hour clocks. M02 Students will be expected to read and record calendar dates in a variety of formats.			

	<ul> <li>M02 Students will be expected to relate the number of seconds to a minute, the numbers of minutes to an hour, the numbers of hours to a day, and the number of days to a month in a problem-solving context.</li> <li>M02.01: Determine the number of days in any given month using a calendar.</li> <li>M02.02: Solve a given problem involving the number of seconds in a minute, the number of minutes in an hour, the number of hours in a day, or the number of days in a given month.</li> <li>M02.03: Create a calendar that includes days of the week, dates, and personal events.</li> </ul>		
MEASUREMENT - CIRCLES			<ul> <li>M01 Students will be expected to demonstrate an understanding of circles by</li> <li>describing the relationships among radius, diameter, and circumference</li> <li>relating circumference to pi</li> <li>determining the sum of the central angles</li> <li>constructing circles with a given radius or diameter</li> <li>solving problems involving the radii, diameters, and circumferences of circles.</li> </ul>
MEASUREMENT - TRIANGLES			

	GEOMETRY PROGRESSION							
ΤΟΡΙΟ	MATHEMATICS 3	MATHEMATICS 4	MATHEMATICS 5	MATHEMATICS 6	MATHEMATICS 7			
3-D OBJECTS	<b>G01</b> Students will be expected to describe 3-D objects according to the shape of the faces and the number of edges and vertices.	<b>G01</b> Students will be expected to describe and construct rectangular and triangular prisms.	<b>G01</b> Students will be expected to describe and provide examples of edges and faces of 3-D objects, and sides of 2-D shapes that are parallel, intersecting, perpendicular, vertical, and horizontal.	<ul> <li>M03 Students will be expected to develop and apply a formula for determining the</li> <li>perimeter of polygons</li> <li>area of rectangles</li> <li>volume of right rectangular prisms</li> </ul>				

	G01.01: Identify the faces, edges, and vertices of given 3-D objects, including spheres, cones, cylinders, pyramids, cubes and other prisms. G01.02: Identify the shape of the faces of a given 3-D object. G01.03: Determine the number of faces, edges, and vertices of a given 3-D object. G01.04: Sort a given set of 3-D objects according to the number of faces, edges, or vertices.				
2-D SHAPES	<ul> <li>G02 Students will be expected to name, describe, compare, create, and sort regular and irregular polygons, including triangles, quadrilaterals, pentagons, hexagons, and octagons according to the number of sides.</li> <li>G01 Students will be expected to describe 3-D objects according to the shape of the faces and the number of edges and vertices.</li> </ul>	<ul> <li>G02 Students will be expected to demonstrate an understanding of congruency, concretely and pictorially.</li> <li>G03 Students will be expected to demonstrate an understanding of line symmetry by <ul> <li>identifying symmetrical 2-D shapes</li> <li>creating symmetrical 2-D shapes</li> <li>drawing one or more lines of symmetry in a 2-D shapes</li> </ul> </li> </ul>	<ul> <li>G01 Students will be expected to describe and provide examples of edges and faces of 3-D objects, and sides of 2-D shapes that are parallel, intersecting, perpendicular, vertical, and horizontal.</li> <li>G02 Students will be expected to name, identify, and sort quadrilaterals, including rectangles, squares, trapezoids, parallelograms, and rhombi, according to their attributes.</li> </ul>	<ul> <li>M03 Students will be expected to develop and apply a formula for determining the <ul> <li>perimeter of polygons</li> <li>area of rectangles</li> <li>volume of right rectangular prisms</li> </ul> </li> <li>G01 Students will be expected to construct and compare triangles, including scalene, isosceles, equilateral, right, obtuse, or acute in different orientations.</li> <li>G02 Students will be expected to describe and compare the sides and angles of regular and irregular polygons.</li> </ul>	<ul> <li>G01 Students will be expected to perform geometric constructions, including</li> <li>perpendicular line segments</li> <li>parallel line segments</li> <li>perpendicular bisectors</li> <li>angle bisectors</li> <li>M02 Students will be expected to develop and apply a formula for determining the area of triangles, parallelograms, and circles.</li> </ul>
ANGLES			<b>G05</b> Students will be expected to identify right angles.	<ul> <li>M01 Students will be expected to demonstrate an understanding of angles by</li> <li>identifying examples of angles in the environment</li> <li>classifying angles according</li> <li>to their measure</li> <li>estimating the measure of angles using 45°, 90°, and</li> <li>180° as reference angles</li> <li>determining angle measures in degrees</li> <li>drawing and labelling</li> <li>angles when the measure is specified</li> </ul>	

SORTING 3-D OBJECTS AND 2-D SHAPES	<b>G02</b> Students will be expected to name, identify, and sort quadrilaterals, including rectangles, squares, trapezoids, parallelograms, and rhombi, according to their attributes.	<b>M02</b> Students will be expected to demonstrate that the sum of interior angles is 180° in a triangle and 360° in a quadrilateral.	
TRANSFORMATI ONAL GEOMETRY	G03 Students will be expected to perform a single transformation (translation, rotation, or reflection) of a 2-D shape (with and without technology) and draw and describe the image. G04 Students will be expected to identify and describe a single transformation, including a translation, rotation, and reflection of 2-D shapes.	<ul> <li>G03 Students will be expected to perform a combination of translation(s), rotation(s), and/or reflection(s) on a single 2-D shape, with and without technology, and draw and describe the image.</li> <li>G04 Students will be expected to perform a combination of successive transformations of 2-D shapes to create a design and identify and describe the transformations.</li> <li>G05 Students will be expected to identify and plot points in the first quadrant of a Cartesian plane using whole number ordered pairs.</li> <li>G06 Students will be expected to perform and describe single transformations of a 2-D shape in the first quadrant of a Cartesian plane (limited to whole number vertices).</li> </ul>	<ul> <li>GO2 Students will be expected to identify and plot points in the four quadrants of a Cartesian plane, using integral ordered pairs.</li> <li>GO2.01 Label the axes of a four quadrant Cartesian plane and identify the origin.</li> <li>GO2.02 Identify the location of a given point in any quadrant of a Cartesian plane using an integral ordered pair.</li> <li>GO2.03 Plot the point corresponding to a given integral ordered pair on a Cartesian plane with units of 1, 2, 5, or 10 on its axes.</li> <li>GO2.05 Create shapes and designs in a Cartesian plane using given integral ordered pairs.</li> <li>GO2.05 Create shapes and designs, and identify the points used to produce the shapes and designs, in any quadrant of a Cartesian plane.</li> <li>GO3 Students will be expected to perform and describe transformations (translations, rotations, or reflections) of a 2-D shape in all four quadrants of a Cartesian plane (limited to integral number vertices).</li> </ul>

	1		PROBABILITY PROGRESSION	1	
TOPIC	MATHEMATICS 3	MATHEMATICS 4	MATHEMATICS 5	MATHEMATICS 6	MATHEMATICS 7
DATA MANAGEMENT	<b>SP01</b> Students will be expected to collect first-hand data and organize it using tally marks, line plots, charts, and lists to answer questions.	<b>SP01</b> Students will be expected to demonstrate an understanding of many-to-one correspondence.	<b>SP01</b> Students will be expected to differentiate between first-hand and second-hand data.	<b>G05</b> Students will be expected to identify and plot points in the first quadrant of a Cartesian plane using whole number ordered pairs.	<b>G02</b> Students will be expected to identify and plot points in the four quadrants of a Cartesian plane, using integral ordered pairs.
	SP02 Students will be expected to construct, label, and interpret bar graphs to solve problems.	SP02 Students will be expected to construct and interpret pictographs and bar graphs involving many-to-one correspondence to draw conclusions.	SP02 Students will be expected to construct and interpret double bar graphs to draw conclusions. SP02.01 Determine the attributes (title, axes, intervals, and legend) of double bar graphs by comparing a given set of double bar graphs. SP02.02 Represent a given set of data by creating a double bar graph, label the title and axes, and create a legend without the use of technology. SP02.03 Draw conclusions from a given double bar graph to answer questions. SP02.04 Identify examples of double bar graphs used in a variety of print and electronic media, such as newspapers, magazines, and the Internet. SP02.05 Solve a given problem by constructing and interpreting a double bar graph	<ul> <li>SP01 Students will be expected to create, label, and interpret line graphs to draw conclusions.</li> <li>SP02 Students will be expected to select, justify, and use appropriate methods of collecting data, including questionnaires, experiments, databases, and electronic media.</li> <li>SP03 Students will be expected to graph collected data and analyze the graph to solve problems.</li> </ul>	<ul> <li>G02.01 Label the axes of a four quadrant Cartesian plane and identify the origin.</li> <li>G02.02 Identify the location of a given point in any quadrant of a Cartesian plane using an integral ordered pair.</li> <li>G02.03 Plot the point corresponding to a given integral ordered pair on a Cartesian plane with units of 1, 2, 5, or 10 on its axes.</li> <li>G02.04 Draw shapes and designs in a Cartesian plane using given integral ordered pairs.</li> <li>G02.05 Create shapes and designs, and identify the points used to produce the shapes and designs, in any quadrant of a Cartesian plane.</li> <li>SP03 Students will be expected to construct, label, and interpret circle graphs to solve problems.</li> <li>SP03.01 Identify common attributes of circle graphs, such as</li> <li>title, label, or legend</li> <li>the sum of the central angles is 3600</li> <li>the data is reported as a percent of the total, and the sum of the percents is equal to 100%</li> <li>SP03.02 Create and label a circle graph, with and without technology, to display a given set of data.</li> </ul>

				SP03.03 Find and compare circle graphs in a variety of print and electronic media, such as newspapers, magazines, and the Internet. SP03.04 Translate percentages displayed in a circle graph into quantities to solve a given problem. SP03.05 Interpret a given or constructed circle graph to answer questions.
STATISTICS				<ul> <li>SP01 Students will be expected to demonstrate an understanding of central tendency and range by</li> <li>determining the measures of central tendency (mean, median, mode) and range</li> <li>determining the most appropriate measures of central tendency to report findings</li> <li>SP02 Students will be expected to determine the effect on the mean, median, and mode when an outlier is included in a data set.</li> </ul>
PROBABILITY		<ul> <li>SP03 Students will be expected to describe the likelihood of a single outcome occurring, using words such as impossible, possible, and certain.</li> <li>SP04 Students will be expected to compare the likelihood of two possible outcomes occurring, using words such as less likely, equally likely, or more likely.</li> </ul>	<ul> <li>SP04 Students will be expected to demonstrate an understanding of probability by</li> <li>identifying all possible outcomes of a probability experiment</li> <li>differentiating between experimental and theoretical probability</li> <li>determining the theoretical probability experiment</li> <li>determining the theoretical probability experiment</li> <li>determining the experimental probability of outcomes in a probability of outcomes in a probability experiment</li> <li>comparing experimental results with the theoretical probability for an experiment</li> </ul>	<ul> <li>SP04 Students will be expected to express probabilities as ratios, fractions, and percents.</li> <li>SP05 Students will be expected to identify the sample space (where the combined sample space has 36 or fewer elements) for a probability experiment involving two independent events.</li> <li>SP06 Students will be expected to conduct a probability experiment to compare the theoretical probability (determined using a tree diagram, table, or other graphic organizer) and experimental probability of two independent events.</li> </ul>